The problem of biology is not to stand aghast at the complexity but to conquer it. Sydney Brenner.

# Abstract Machines of Systems Biology

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Microsoft Research

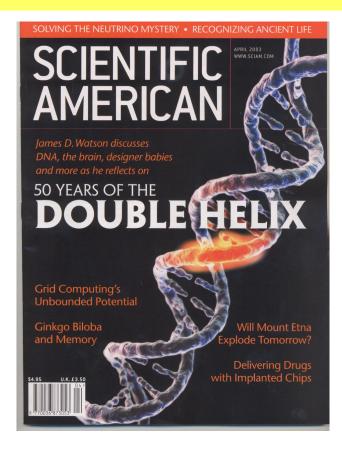
Open Lectures for PhD Students in Computer Science Warsaw 2009-03-12..13

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## 50 Years of Molecular Cell Biology

### • Genes are made of DNA

- Store digital information as sequences of 4 different nucleotides
- Direct protein assembly through RNA and the Genetic Code
- Proteins (>10000) are made of amino acids
  - Process signals
  - Activate genes
  - Move materials
  - Catalyze reactions to produce substances
  - Control energy production and consumption
- Bootstrapping still a mystery
  - DNA, RNA, proteins, membranes are today interdependent. Not clear who came first
  - Separation of tasks happened a long time ago
  - Not understood, not essential



### **Towards Systems Biology**

- Biologists now understand many of the cellular components
  - $\circ$  A whole team of biologists will typically study a single protein for years
  - Reductionism: understand the components in order to understand the system
- But this has not led to understand how "the system" works
  - Behavior comes from complex patterns of interactions between components
  - $\circ$  Predictive biology and pharmacology still rare
  - Synthetic biology still unreliable
- New approach: try to understand "the system"
  - Experimentally: massive data gathering and data mining (e.g. Genome projects)
  - Conceptually: modeling and analyzing networks (i.e. interactions) of components

### • What kind of a system?

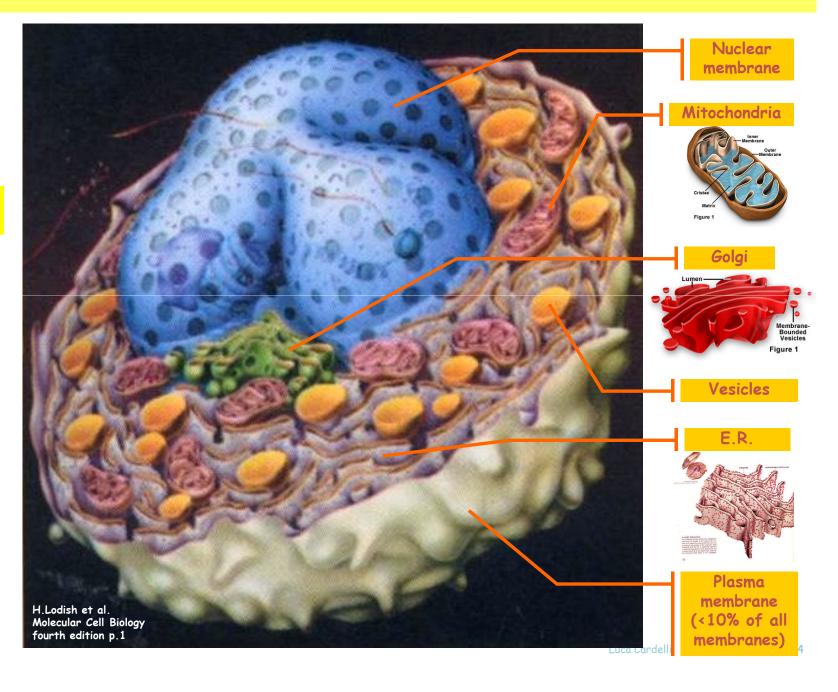
- Just beyond the basic chemistry of energy and materials processing...
- Built right out of digital information (DNA)
- o Based on information processing for both survival and evolution
- *Highly* concurrent
- Can we fix it when it breaks?
  - Really becomes: How is information structured and processed?

### **Structural Architecture**

Eukaryotic Cell

(10~100 trillion in human body)

Membranes everywhere

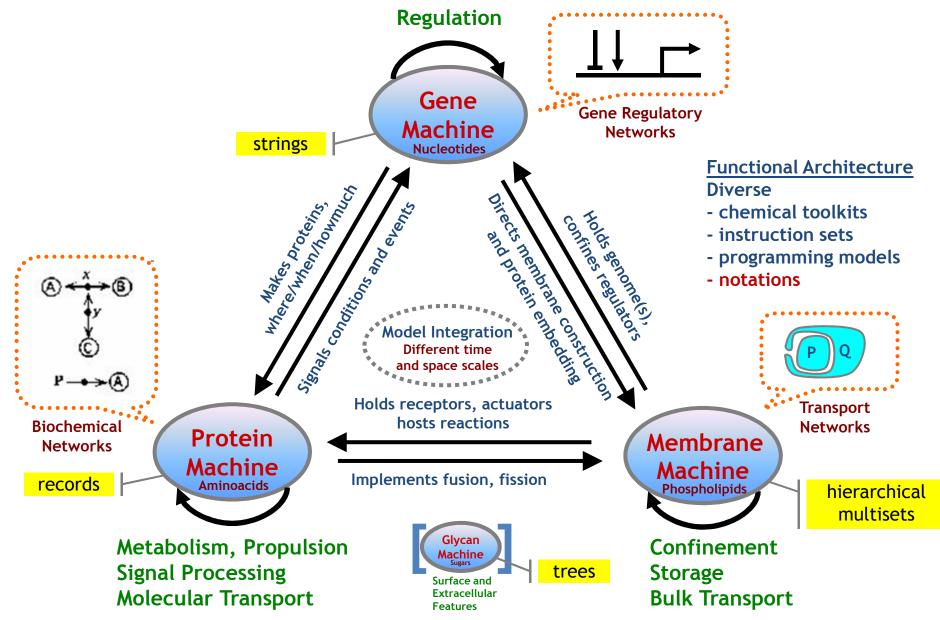




# **Modeling It**

- Even if we understood it, how would we model it?
  - Millions of differential equations? Hmmm...
  - Highly, *highly*, concurrent and asynchronous
  - $\circ$  Stochastic (nondeterministic and discontinuous)
- And we will have to model it in order to understand it.
  - $\circ~$  Simulation and analysis are key to understanding interactions
- What's peculiar about these systems?
  - $\circ~$  They are huge and complicated
  - They are concurrent and unpredictable
  - There is no documentation
  - $\circ$  We understand them by looking at traces and dumps

### **Abstract Machines of Systems Biology**

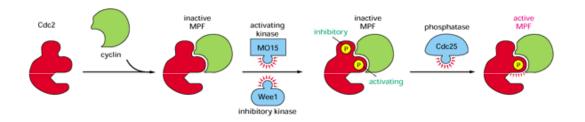


# **The Protein Machine**

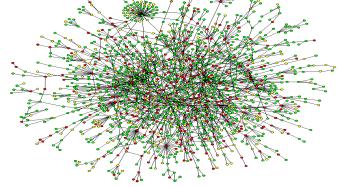
# 1. The Protein Machine

# Very close to the atoms.

- Complex folded-up shapes that:
  - $\circ~$  Fit together, dock, undock.
  - $\circ~$  Excite/unexcite, warp each other.
  - $\circ$  Bring together, catalyze, transform materials.
  - $\circ~$  Form complex aggregates and networks.



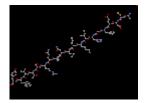
- Mapping out such networks:
  - In principle, it's "just" a very large set of chemical equations.
  - Notations have been developed to summarize and abstract.



A molecular interaction network. (Nodes are distinct protein kinds, arcs mean that two kinds of proteins interact.)

### **Protein Structure**

Primary

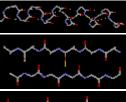


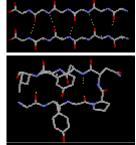
The 20 Aminoacids



Tryptophan

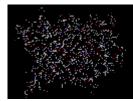
#### Secondary

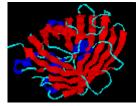




Alpha Helix, Beta Sheet

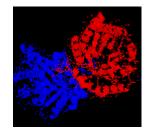
#### Tertiary





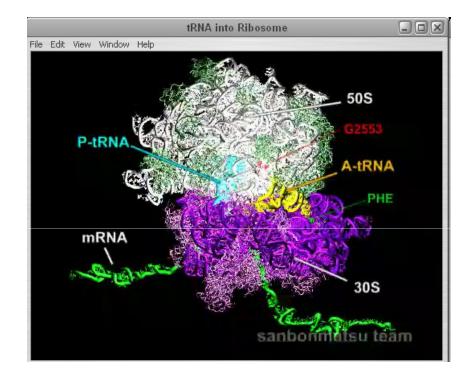
Green Fluorescent Protein

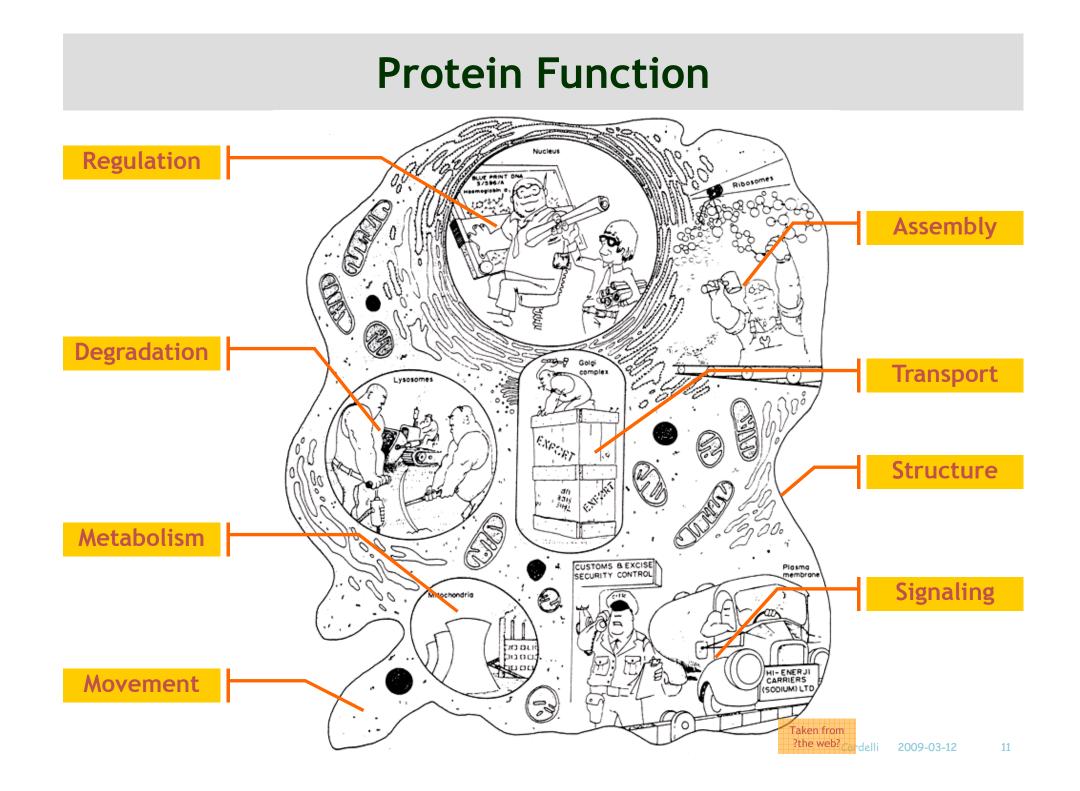
### Quaternary



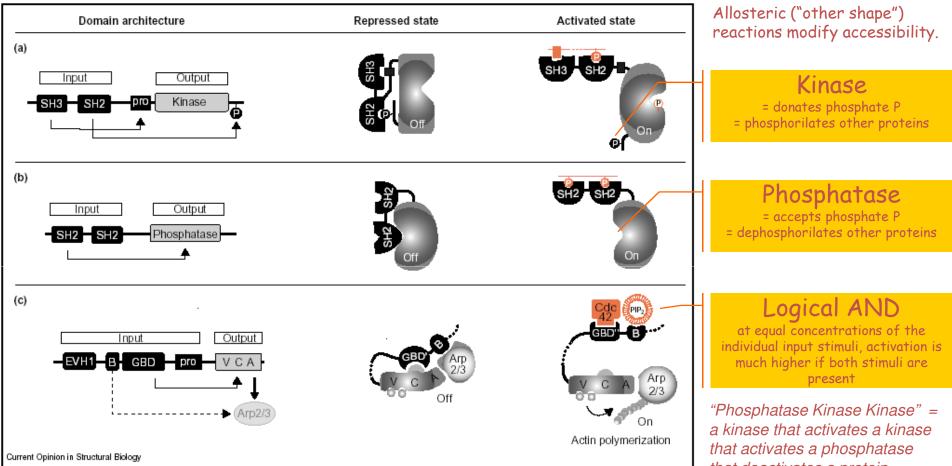
#### Triose Phosphate Isomerase

### **Ribosome: mRNA to Protein**





### Some Allosteric Switches



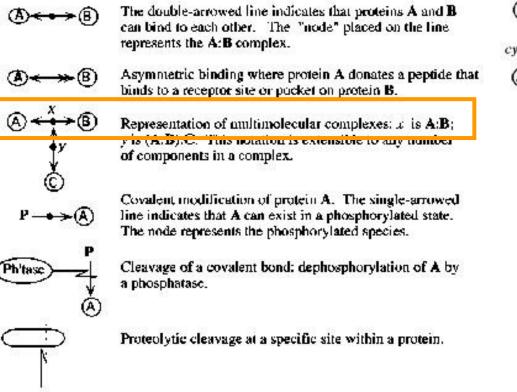
Domain architecture and autoinhibitory interactions in modular switch proteins. (a) Src family kinases contain N-terminal SH3 and SH2 domains, and a kinase domain flanked by intramolecular SH3-binding and SH2-binding sites (when the C-terminal motif tyrosine is phosphorylated by Csk). The crystal structures of several family members show that both intramolecular domain interactions function in concert to lock the kinase in an inactive conformation. Activating stimuli (red) include external SH2 or SH3 ligands. After initial activation, the kinase is maintained in an active state by autophosphorylation of its activation loop. (b) SHP-2 phosphatase contains two SH2 domains and a phosphatase domain. The crystal structure of the phosphatase

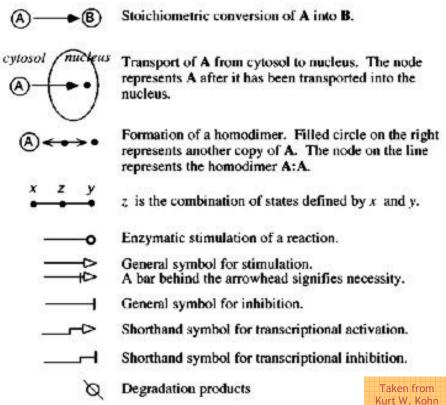
shows that the N-terminal SH2 domain participates in an autoinhibitory interaction that directly blocks the phosphatase active site. Binding of external SH2 ligands activates by disrupting the autoinhibitory interaction. (c) N-WASP contains an Enabled VASP homology 1 (EVH1) domain, a B motif, a GBD, a proline-rich segment (pro) and an output region (VCA) that alone binds the Arp2/3 complex and stimulates its actin nucleation activity. The B and GBD motifs are required to repress activity and, by current models, are thought to participate in intracomplex interactions (only the structure of the GBD intramolecular complex for WASP is known). GTP-bound Cdc42 and PIP<sub>2</sub> synergistically activate N-WASP.

that deactivates a protein.

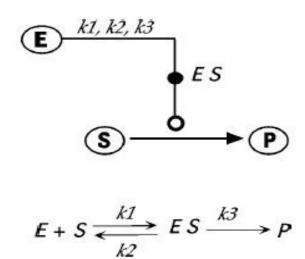
Humans have the same number of modular protein domains (building blocks) as worms, but twice the number of multi-domain proteins.

### MIM: Molecular Interaction Maps (Kohn)





### Kohn Diagrams



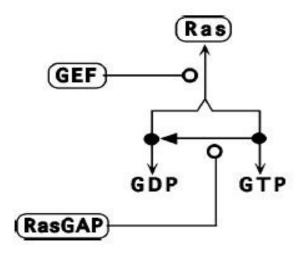


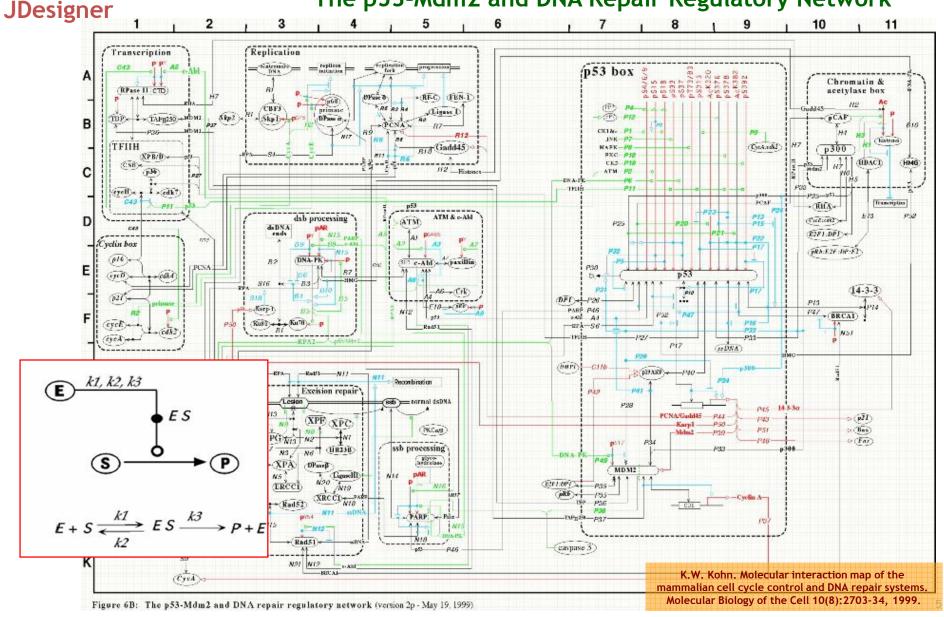
FIG. 3. Simple one-way enzymatic reaction. (If there is an energy source, such as ATP hydrolysis, it can be omitted when ATP concentration is not an important factor.) In explicit formulations, the reaction identifiers or rate constant designations can be placed on the enzyme reaction line, and the node ES can identify the enzyme-substrate species.

FIG. 4. Interconversions between the GTP- and GDP-bound states of Ras. (1) GDP and GTP compete with each other for binding to a site on Ras (this binding is only slowly reversible). (2) GEF (guanine nucleotide exchange factor) facilitates the binding or dissociation of GDP or GTP (the concentration of GTP normally far exceeds that of GDP). (Implicit is the reversible binding between GEF and Ras which opens the binding site for GDP/GTP exchange.) (3) Ras has an intrinsic GTPase activity that slowly converts bound GTP to bound GDP (stoichiometric conversion arrow points from the node representing Ras.GTP to the node representing Ras.GDP). (4) RasGAP (a GTPase activating protein) enhances the GTPase activity of Ras. (Implicit is the reversible enzyme–substrate binding between RasGAP and Ras.)

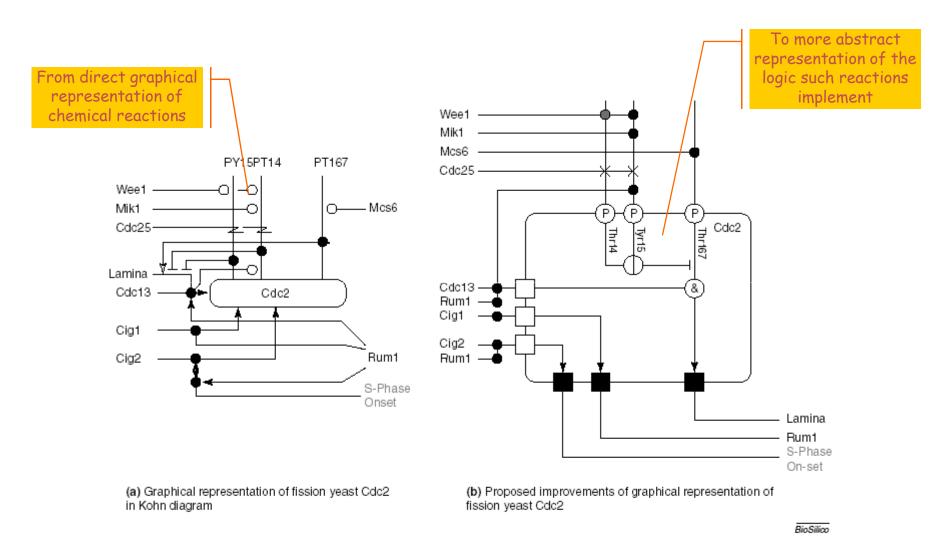
### Molecular Interaction Maps (Kohn)

http://www.cds.caltech.edu/~hsauro/index.htm

### The p53-Mdm2 and DNA Repair Regulatory Network



### **Kitano Diagrams**



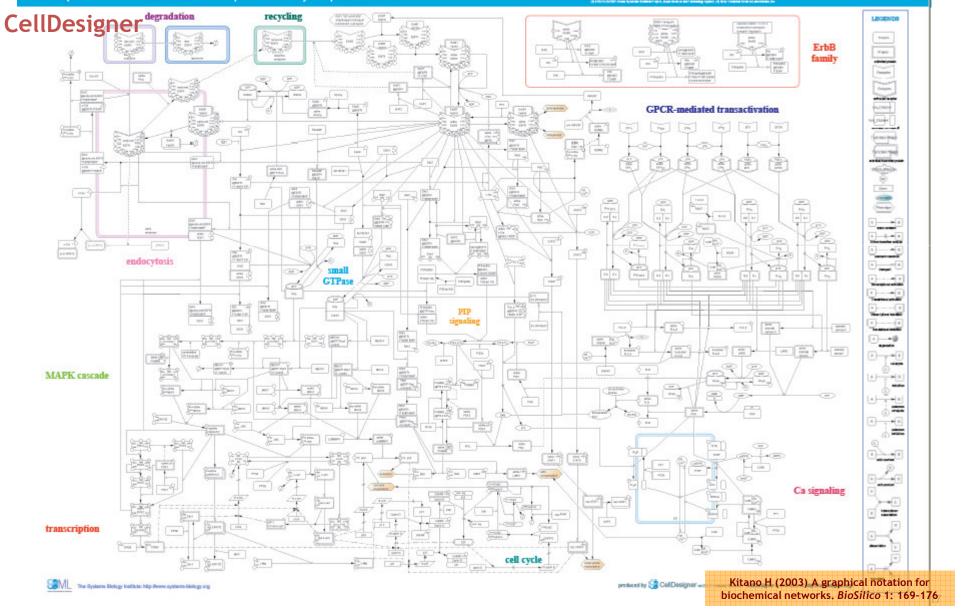
**Figure 1.** Representation of fission yeast Cdc2 protein in (a) the original MIM and (b) proposed improvements. Both diagrams represent interactions involving fission yeast Cdc2. Weel phosphorylates Thr14 and Tyr15, Mik1 phosphorylates Tyr15, Mcs6 phosphorylates Thr167, and Cdc25 dephosphorylates Thr14 and Tyr15. Cdc2 binds to either Cdc13, Cig1, or Cig2. When Cdc2 is forming a complex with Cdc13 and only Thr167 is phosphorylated, the complex interacts with Lamina. Phosphorylation of either Thr14 or Tyr15 inhibits activation of Cdc2 due to phosphorylates Tyr15 of its Cdc2. The complex of Cdc2 and Cig1 interacts with Rum1. Cdc2-Cdc13 complex and Cdc-Cig2 complex form heterotrimers involving Rum1.



### **Molecular Interaction Maps (Kitano)**

Epidermal Growth Factor Receptor Pathway Map

Kanase Orda (17), Yulidiko Mahazaka (2), Hinsaki Kitano (174) (3) (a kuta kata waka, (2) antara kata kata kata ata kata ya kata kata)



### **Molecular Interaction Maps (Kitano)**

#### A comprehensive pathway map of epidermal growth factor receptor signaling

Epidermal Growth Factor Receptor Pathway Map concernant

Kanae Oda<sup>1,2</sup>, Yukiko Matsuoka<sup>1,3</sup>, Akira Funahashi<sup>1,3</sup> and Hiroaki Kitano<sup>1,2,3,4</sup>

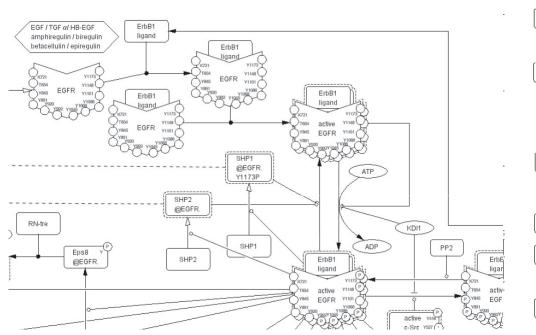
1. The Systems Biology Institute, Tokyo, Japan

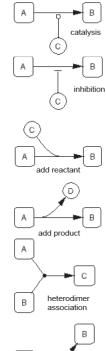
2. Department of Fundamental Science and Technology, Keio University, Tokyo, Japan

3. ERATO-SORST Kitano Symbiotic Systems Project, Japan Science and Technology Agency, Tokyo, Japan

4. Sony Computer Science Laboratories, Inc., Tokyo, Japan

"The current EGFR map is **essentially a state transition diagram**, in which one state of the system is represented in one node, and an arc from one node to another node represents a transition of the state of the system. This class of diagrams is often used in engineering and software development, and the schema avoids using symbols that directly point to molecules to indicate activation or inhibition. "





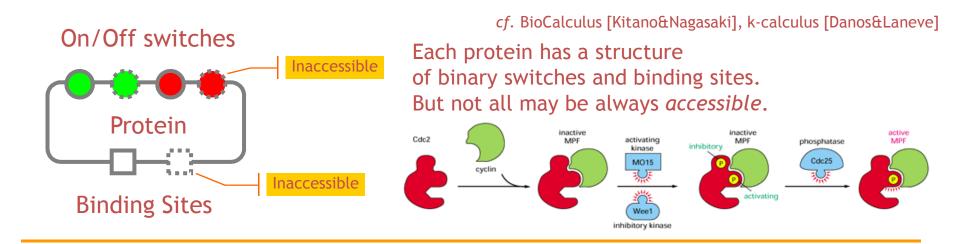
А

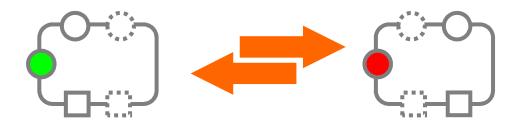
dissociation

С

state transition

### **The Protein Machine "Instruction Set"**



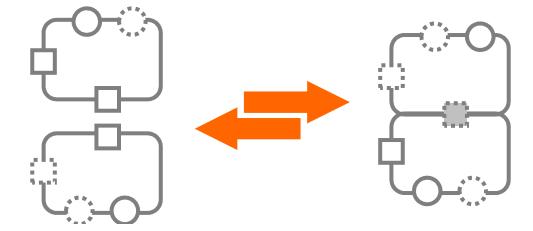


### Switching of accessible switches.

- May cause other switches and

binding sites to become (in)accessible.

- May be triggered or inhibited by nearby specific proteins in specific states.



### Binding on accessible sites.

May cause other switches and binding sites to become (in)accessible.
May be triggered or inhibited by nearby specific proteins in specific states.

### **Notations for the Protein Machine**

- Stochastic *π*-Calculus
  - Priami (following Hillston's PEPA) formalizes a stochastic version of p-calculus where channels have communication *rates*.
- BioSPi
  - Regev-Shapiro-Silverman propose modeling chemical interactions (exchange of electrons and small molecules) as "communication".
  - Standard stochastic simulation algorithms (Gillespie) can be used to run in-silico experiments.
  - Complex formation is encoded via p-restriction.
- PEPA
  - Calder Gilmore and Hillston model the ERK pathway.
- k-calculus
  - Danos and Laneve (following Kitano's BioCalculus) define a calculus where complex formation is primitive.
- (Stochastic) Petri Nets
  - S.Reddy'94 modeling pathways.
  - Srivastava Perterson and Bentley analyze and simulate E.coli stress response circuit.

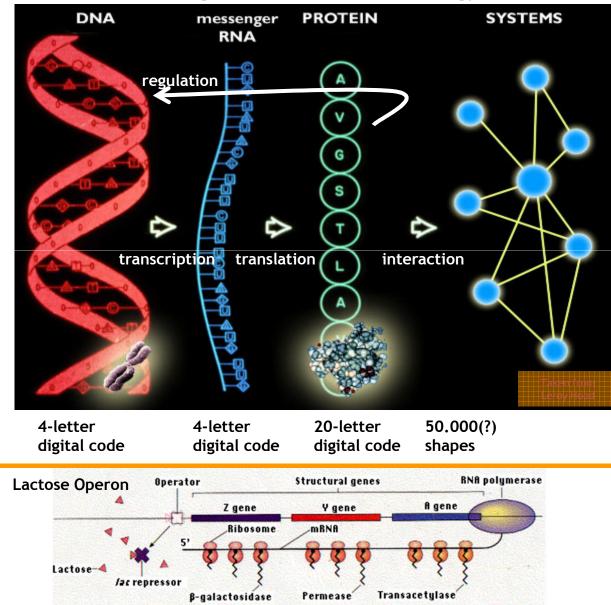
- Bio State Charts
  - Harel uses State Charts to model biological interactions via a semi-graphical FSM notation.
- Pathway Logic
  - Talcott-Eker-Knapp-Lincoln use term-rewriting.
- BioCham
  - ChabrierRivier-Fages-Soliman use term-rewriting and CLT modelchecking.
- Kohn Diagrams, Kitano Diagrams
- SBML (Systems Biology Markup Language)
  - XML dialect for MIM's:
    - Compartments (statically nested)
    - Reagents with concentrations
    - Reactions with various rate laws
  - Read and written by many tools via the Systems Biology Workbench protocol

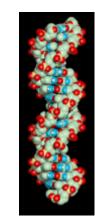
# **The Gene Machine**

# 2. The Gene Machine

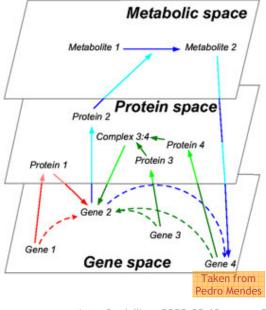
# Pretty far from the atoms.

### The "Central Dogma" of Molecular Biology

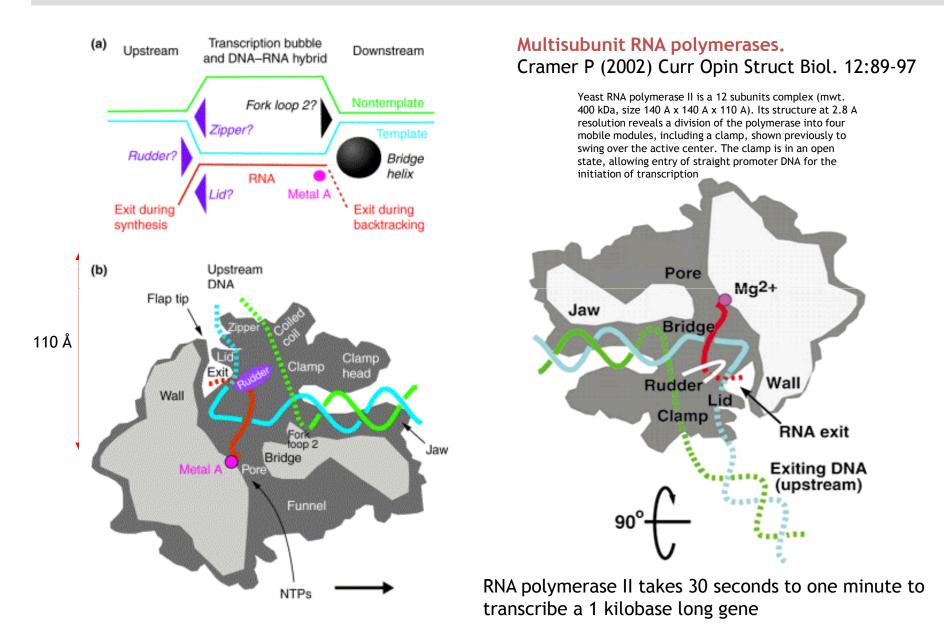




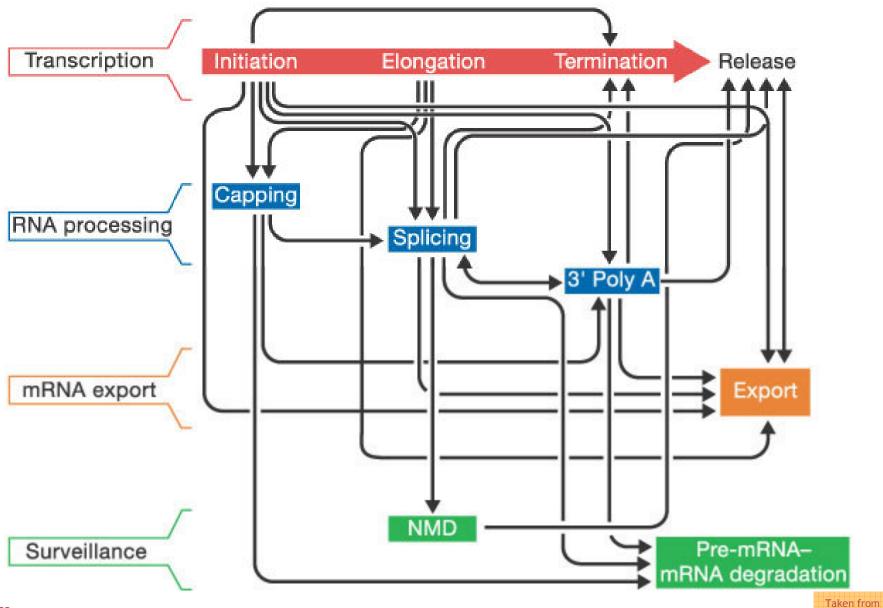
**DNA Tutorial** 



### **RNA Polymerase: DNA to RNA**



## Transcription



???

### Transcription

E. ColiH. SapiensNumber of genes3.20025.000Number of different transcription factors1502:000

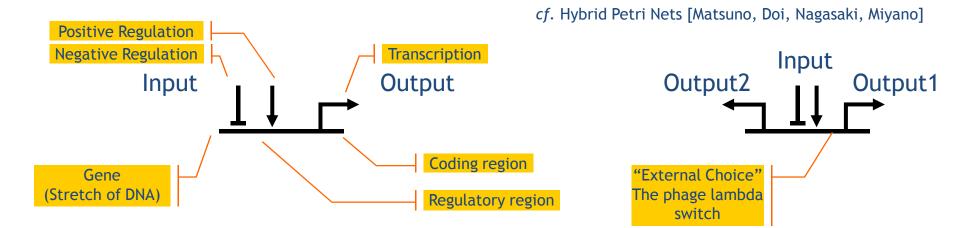
	10 <sup>2</sup> to 10 <sup>3</sup> bp :	400 genes	
Gene	10 <sup>3</sup> to 10 <sup>4</sup> bp :	6000 genes,	1.to.10.minutes
length	10 <sup>4</sup> to 10 <sup>5</sup> bp :	12.200 genes	10 to 100 min
H. Sapiens	10 <sup>5</sup> to 10 <sup>6</sup> bp :	3200 genes	• • • • • • • • • • • • • • • • • • • •
	10 <sup>6</sup> to 2.4 10 <sup>6</sup> bp : 62 genes		16 to 24 h

Number of transcripts per gene : 0,1 to 10<sup>6</sup>. Up to 10<sup>6</sup> mRNA globin in erythroid cells 15.000 mRNA actin / nucleus in muscle fibers 10 to 100 copies for mRNAs encoding transcription factors

In an HeLa cell, there are approx. 100 mol. RNA pol / gene coding rRNA



### **The Gene Machine "Instruction Set"**

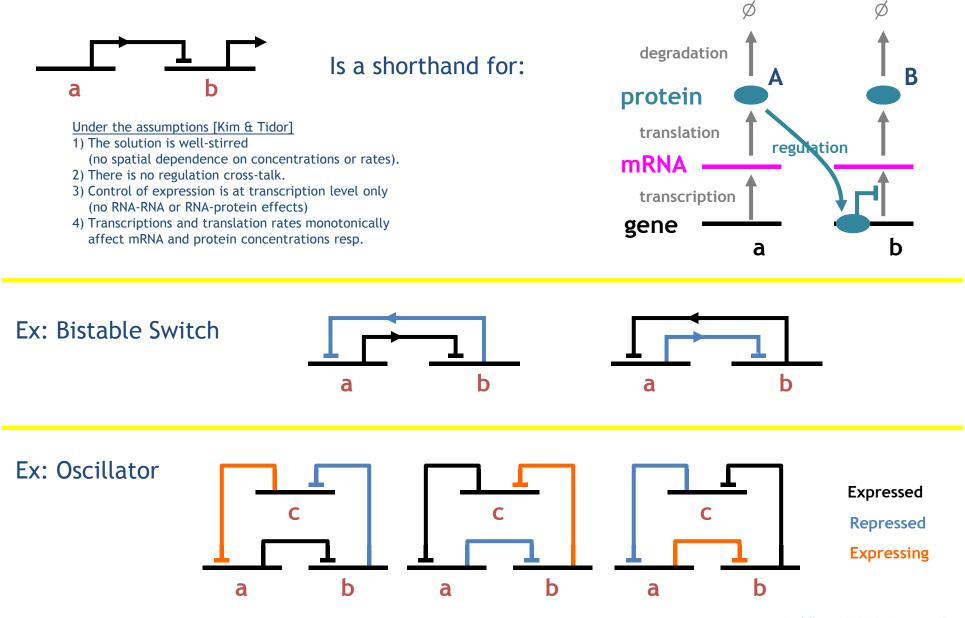


<u>Regulation</u> of a gene (positive and negative) influences transcription. The regulatory region has precise DNA sequences, but not meant for coding proteins: meant for binding regulators.

<u>Transcription</u> produces molecules (RNA or, through RNA, proteins) that bind to regulatory region of other genes (or that are endproducts). Human (and mammalian) Genome Size 3Gbp (Giga base pairs) 750MB @ 4bp/Byte (CD) Non-repetitive: 1Gbp 250MB In genes: 320Mbp 80MB Coding: 160Mbp 40MB Protein-coding genes: 30,000-40,000

<u>M.Genitalium</u> (smallest true organism) 580,073bp 145KB (eBook) <u>E.Coli</u> (bacteria): 4Mbp 1MB (floppy) <u>Yeast</u> (eukarya): 12Mbp 3MB (MP3 song) Wheat 17Gbp 4.25GB (DVD)

### **Gene Composition**



### **Indirect Gene Effects**

No combination of standard high-throughput experiments can reconstruct an a-priori known gene/protein network [Wagner].

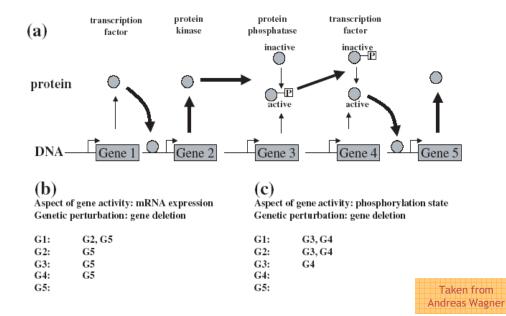
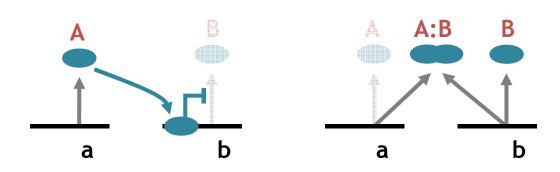
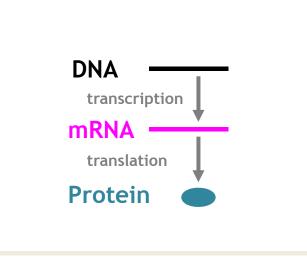


Fig. 1. The importance of specifiying gene activity when reconstructing genetic networks. (a) A hypothetical biochemical pathway involving two transcription factors, a protein kinase, and a protein phosphatase, as well as the genes encoding them. See text for details. (b) Shown is a list of perturbation effects for each of the five genes in (a), when perturbing individual genes by deleting them, and when using mRNA expression level as an indicator of gene activity. The left-most symbol in each line stands for the perturbed gene. To the right of each colon is a list of genes whose activity is affected by the perturbation. (c) Analogous to (b) but for a different notion of gene activity (phosphorylation state).

One of many bistable switches that cannot be described by pure gene regulatory networks [Francois & Hakim].



# Structure of the Coding Region



The Central Dogma

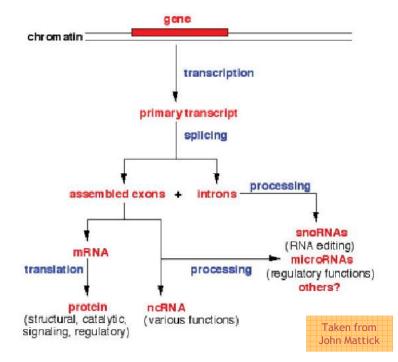
RNA is not just an intermediary; it can:

- Fold-up like a protein
- Act like an enzyme
- Regulate other transcribed RNA
- Direct protein editing

- ...

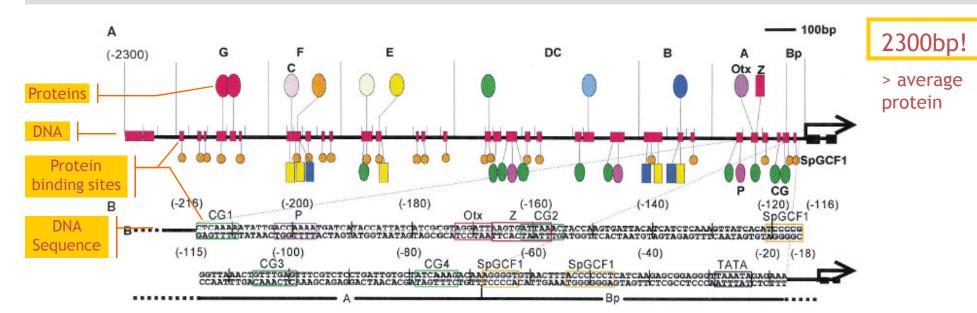
### 97-98% of the transcriptional output of the human genome is non-protein-coding RNA.

30-40,000 "protein genes" (1.5% of genome) 60-100,000 "transcription units" (>30% of genome is transcribed) Challenging the Dogma (in higher organisms)



**Figure 1.** A revised view of the flow of genetic information in the higher eukaryotes. Primary transcripts may be (alternatively) spliced and further processed to produce a range of protein isoforms and/or ncRNAs of various types, which are involved in complex networks of structural, functional and regulatory interactions.

### Structure of a Regulatory Region



#### C Module A functions:

Vegetal plate expression in early development:

Synergism with modules B and G enhancing endoderm expression in later development:

Repression in ectoderm (modules E and F) and skeletogenic mesenchyme (module DC):

#### Modules E, F and DC with LiCI treatment:

**Fig. 1.** Endo 16 cis-regulatory system and interactive roles of module A. (A) Diversity of protein binding sites and organization into modular subregions [modified from (7)]. Specific DNA binding sites are indicated as red blocks; modular subregions are denoted by letters G to A (Bp, basal promoter). Proteins binding at the target sites considered in this work are indicated: Otx, SpOtx-1 (12); SpGCF1 (14); the proteins CG, Z, and P, which are not yet cloned; and protein C [a CREB family protein (18)] in subregion F. Proteins for which sites occur in multiple regions of the DNA sequence (indicated by the black line) are shown beneath. (B) Sequence of module A and location of protein binding sites. Sites are indicated in the same colors as in (A). A fragment containing CG<sub>3</sub> and CG<sub>4</sub> sites as well as Bp has no endoderm-

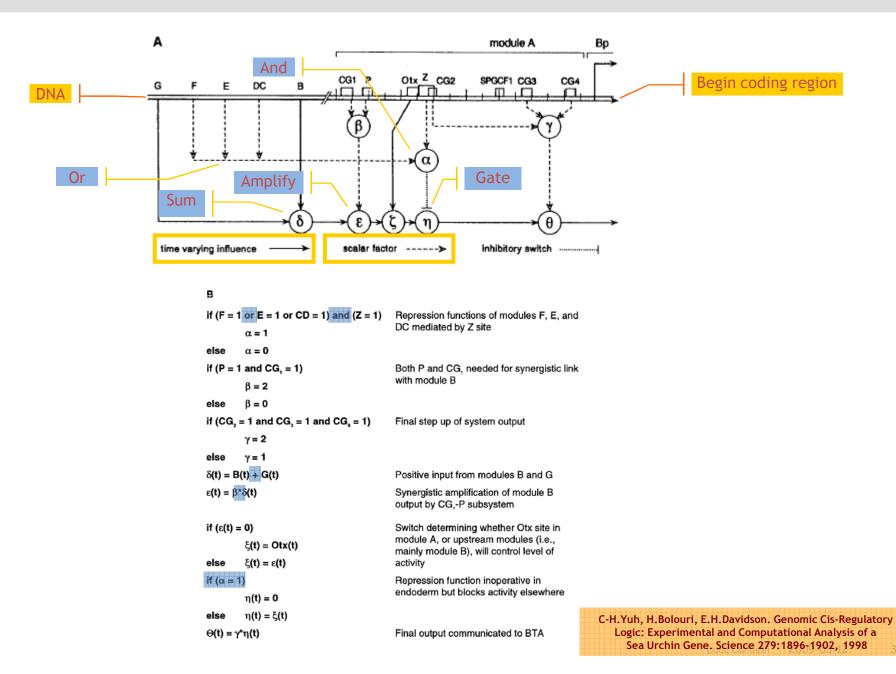
specific activity and services other upstream cis-regulatory systems promiscuously; similarly, the *Endo16* cis-regulatory system functions specifically with heterologous promoters substituted for Bp (*5*, *8*, *19*). Boxed sequences indicate conserved core elements of the target sites (*7*, *12*, *14*), not the complete target site sequences. (**C**) Integrative and interactive functions of module A (*5*, *8*). Module A communicates the output of all upstream modules to the basal transcription apparatus. It also initiates endoderm expression, increases the output of modules B and G, and is required for functions of the upstream modules F, E, and DC. These functions are repression of expression in nonendodermal domains and enhancement of expression in response to LiCl.

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Taken from

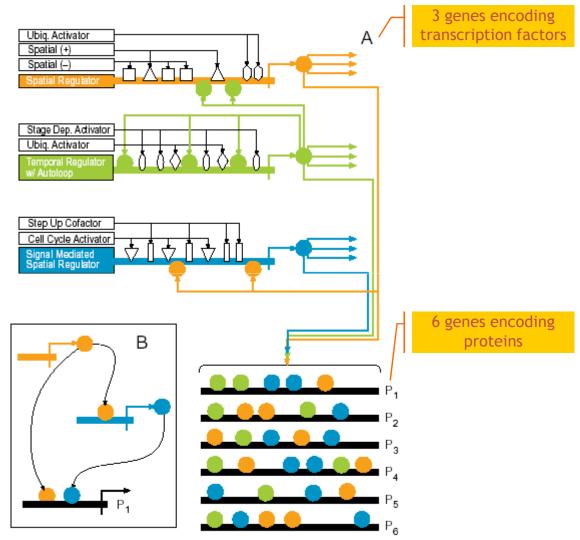
Eric H Davidson

### Function of a Regulatory Region



### **Regulation: Where/When/HowMuch**

Flg. 3. A sector of an imaginary developmental gene regulatory network. (A) Network sector. Three genes encoding transcription factors are shown at the top. These are a spatial regulator (orange), a temporal regulator (green) and a signal-mediated regulator (blue). Genes encoding other transcription factors that originate off the diagram are indicated in black type on open backgrounds. A battery of six genes encoding some differentiation proteins (P1-P6) is shown below. Connections between the three genes encoding transcription factors and target sites in the P1-P6 genes are indicated by respectively colored bent arrows and the transcription factors as solid circles. The spatial regulatory gene is controlled by positive and negative interactions, which establish the limited spatial domain where it will be expressed, and it utilizes a ubiquitous ancillary activator to achieve an appropriate level of expression. This gene would be expressed only at certain stages due to requirement for the factor produced by the green temporal regulator, shown below the line binding to its target sites in the cts-regulatory DNA. The cts-regulatory system of the temporal regulator responds to its own transcription factor, and also depends on a factor appearing only after a certain stage of development, and on another ubiquitous ancillary activator. The signal-mediated regulator produces a factor that is activated by signals. For example, if this were a short-range signal produced by cells adjacent to the domain of expression of the spatial orange regulator, P1-P6 would be expressed only near the boundary. The cts-regulatory system controlling expression of the signalmediated transcription factor includes target sites for the product of the orange spatial regulator, shown binding below the line representing the DNA, and also for two factors that work together to promote transcription during growth, one imagined as a regulator produced when cells are cycling, the other as a ubiquitous co-factor. The arrows at the right indicate that each of the three genes encoding transcription factors have many downstream targets besides the P1-P6 gene battery. Any

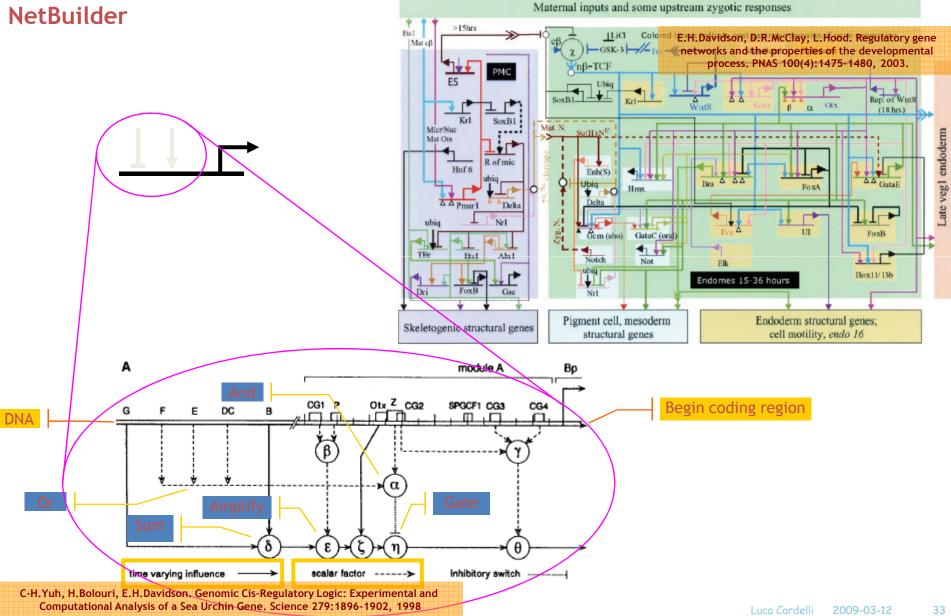


resemblance between this network sector and a known regulatory element is purely coincidental. (B) A single relationship extracted from the network. A causal diagram is shown portraying the multilevel function of the orange spatial regulator, which controls both the gene encoding the blue signal-mediated regulator and the P1 gene; the latter, however, is also directly responsive to the spatial regulator.

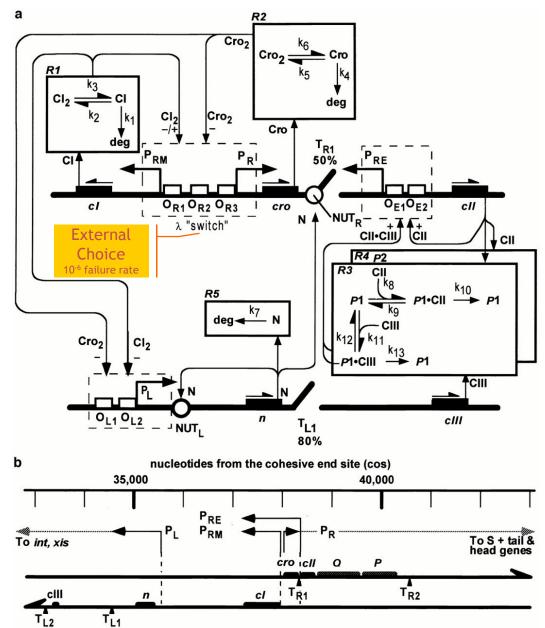
### **Gene Regulatory Networks**

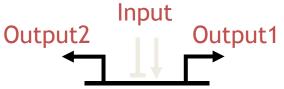
#### http://strc.herts.ac.uk/bio/maria/NetBuilder/

### NetBuilder



### Phage Lambda Decision Circuit





**Figure 1.** The phage lysis-lysogeny decision circuit. (a) Bold horizontal lines indicate stretches of double-stranded DNA. Arrows over genes indicate direction of transcription. Dashed boxes enclose operator sites that comprise a promoter control complex. The three operator sites, OR1-3, of the "lambda switch" implement concentration-dependent logic controlling promoters PRM and PR. Cro and CI dimers bind to the three sites with different affinities and in opposite order to control the activation level of the PRM and PR promoters (PTASHNE 1992 ; SHEA and ACKERS 1985 ). The five boxes R1-R5 contain nongenetic protein reaction subsystems. In R1, R2, and R5, "deg" indicates degradation. When protein N is available, transcribing RNAPs can be antiterminated at the NUTR and NUTL sites; termination sites TR1 and TL1 are inoperative for antiterminated RNAPs. The CI dimer acts as either a repressor or activator of promoter PRM, depending on its concentration. See text for discussion of the proteases labeled as P1 and P2 in R3 and *R*4. (b) decision circuit DNA organization. Phage-encoded genetic elements of the decision circuit are located in a 5000 nucleotide region of the phage DNA. Genes are separated onto leftward and rightward transcribed strands as indicated by the arrows. Rightward extensions of the antiterminated *P*R transcript transcribe the O and P genes essential for phage genome replication and the Q gene that controls transcription of later genes on the lytic pathway. Leftward extension of the antiterminated *PL* transcript transcribes xis and int genes essential for phage chromosome integration and excision into and out of the host chromosome. Locations of four termination sites are indicated by TR1-2 and TL1-2. Taken from Luca Cardelli 2009-03-12 Adam Arkin

### **Whole Genome Activity**

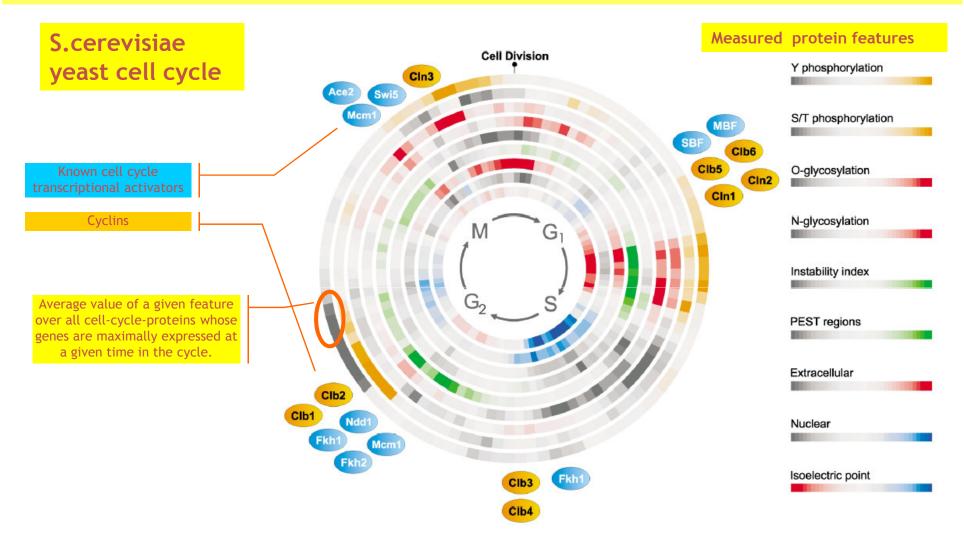


Figure 6. Feature variation during the cell cycle. The temporal variation in nine selected protein features during the cell cycle, with zero time (at the top of the plot) corresponding to the presumed time of cell division (M=G1 transition). The color scales correspond to +/-two standard deviations from the cell cycle average. The concentric feature circles correspond to: isoelectric point, nuclear and extracellular localization predictions, PEST regions, instability index, N-linked glycosylation potential, O-GaINAc glycosylation potential, serine/threonine phosphorylation potential and tyrosine phosphorylation potential. The presumed positions of the four cell cycle phases G1; 5, G2 and M are marked. Also depicted are known cell cycle transcriptional activators (marked in blue), positioned at the time where they are reported to function.

Protein Feature Based Identification of Cell Cycle Regulated Proteins in Yeast

Ulrik de Lichtenberg, Thomas S. Jensen, Lars J. Jensen and Søren Brunak



## The Programming Model

- Strange facts about genetic networks:
  - Not an operator algebra. The output of each gate is fixed and pre-determined; it is never a function of the input!
  - Not term-rewriting, nor Petri nets. Inhibition is widespread.
  - Not Communicating Sequential Processes. Feedback is widespread: asynchronous communication needed to avoid immediate self-deadlocks. Even the simplest gates cannot be modeled as a single synchronous automaton.
  - Not Message-Passing between genes. Messages themselves have behavior (e.g., they stochastically decay and combine), hence messages are processes as well.
  - Not Data-Flow. Any attempt to use data-flow-style modeling seems doomed because of widespread loops that lead to deadlocks or unbounded queues. Data-flow tokens do not "decay" like proteins.
- How can it possibly work?
  - Stochastic broadcasting. The apparently crude idea of broadcasting a whole bunch of asynchronous decaying messages to activate a future gate, means there are never any "pipeline full" deadlocks, even in presence of abundant feedback loops.
  - Stochastic degradation. Degradation is fundamental for system stability, and at the same time can lead to sudden instability and detection of concentration levels.

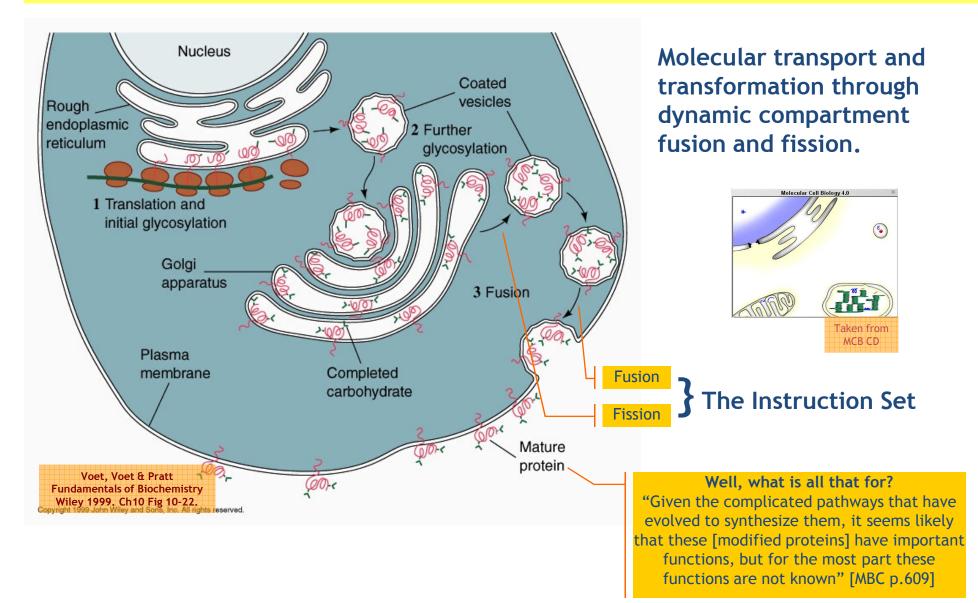
# **Notations for the Gene Machine**

- Many of the same techniques as for the Protein Machine apply.
  - Process Calculi, Petri Nets, Term-Rewriting Systems...
- But the "programming model" is different.
  - Asynchronous stochastic control.
  - Biologically poorly understood.
  - Network "motifs" are being analyzed.

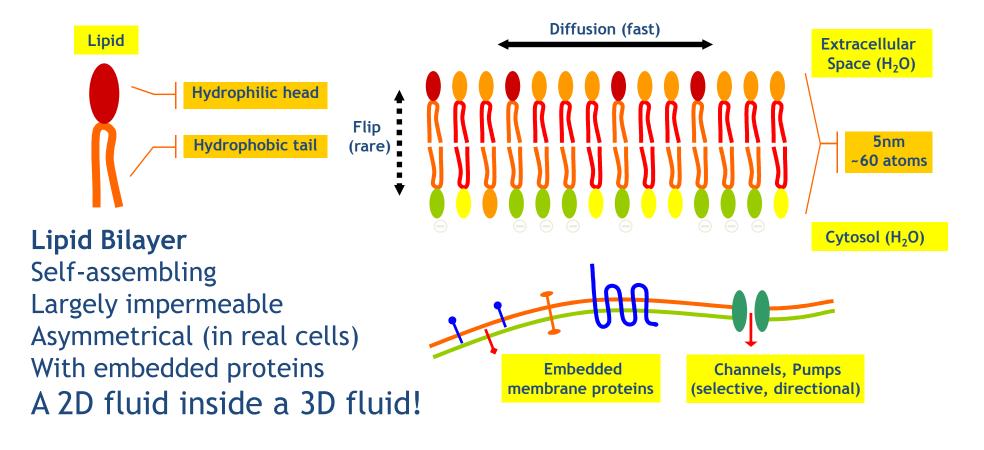
- Specific techniques
  - Hybrid Petri Nets
    - [Matsuno, Doi, Nagasaki, Miyano]
       Gene Regulation
    - Genomic Object Net www.genomicobject.net
- Gene Regulation Diagrams
- Mixed Gene-Protein Diagrams

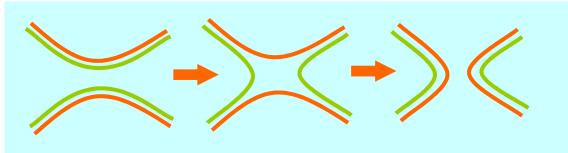
# **The Membrane Machine**

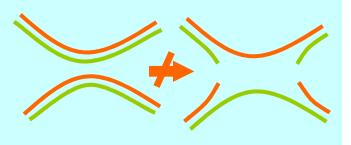
# 3. The Membrane Machine Very far from the atoms.



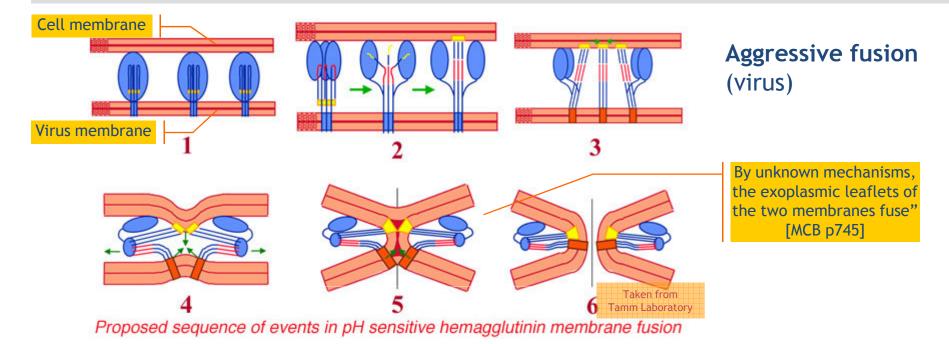
# **Membranes are Oriented 2D Surfaces**







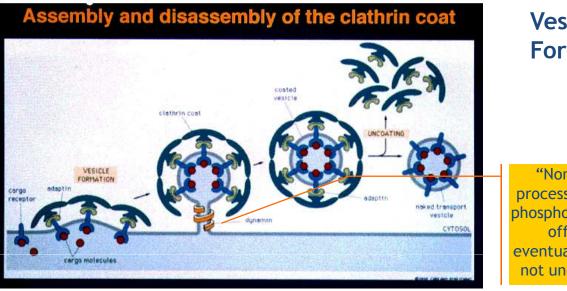
# **Membrane Fusion**



Cooperative fusion (vesicle) "Fusion of the two membranes immediately follows prefusion, but precisely how this occurs is not known" [MCB p742]

# **Membrane Fission**

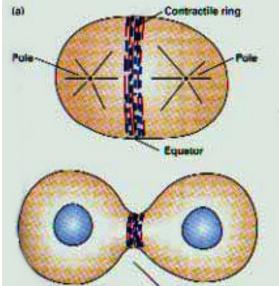
Negative curvature to Positive curvature transition in 3D



#### Vesicle Formation



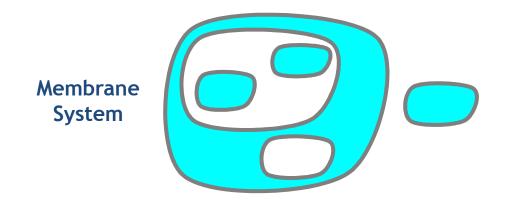
"Nonetheless, the actual process whereby a segment of phospholipid bilayer is 'pinched off' to form a pit and eventually a new vesicle is still not understood" [MCB p.746]



Cleavage furrow

### Cytokinesis (Mitosis)

# **Local Membrane Reactions**

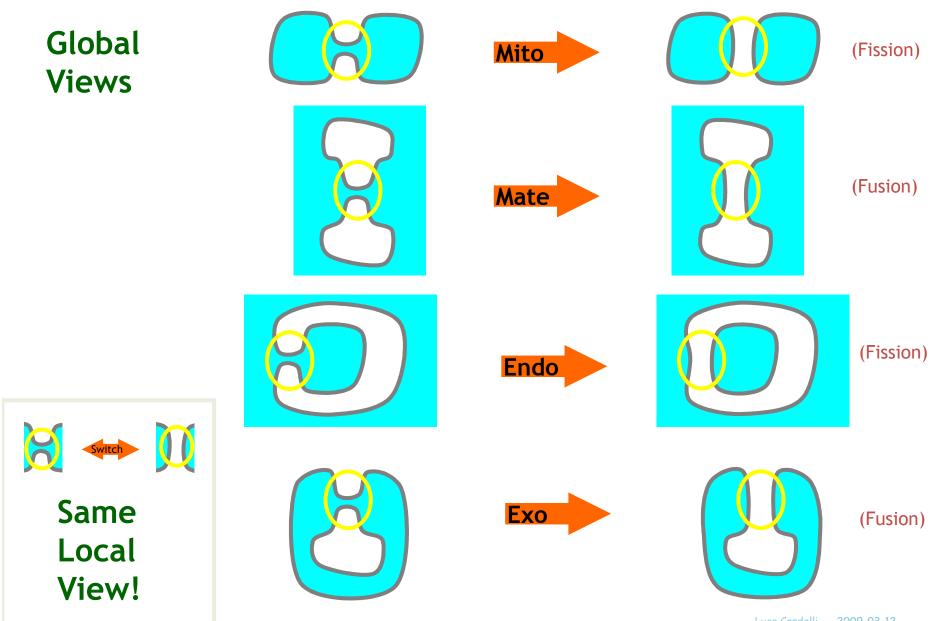


Local View

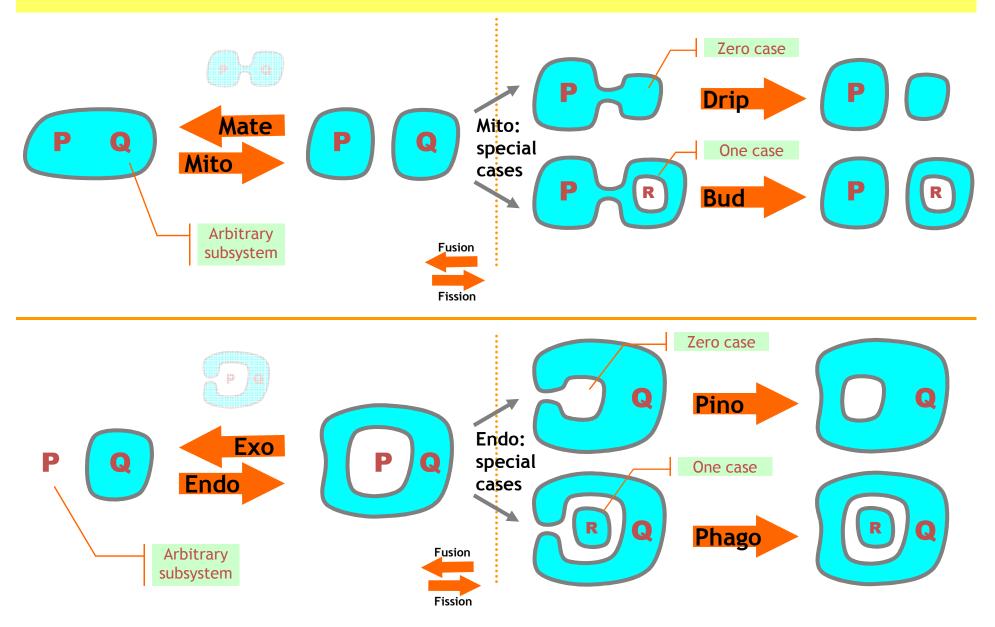


(Symmetric by 90° rotation.)

# **Global Membrane Reactions**

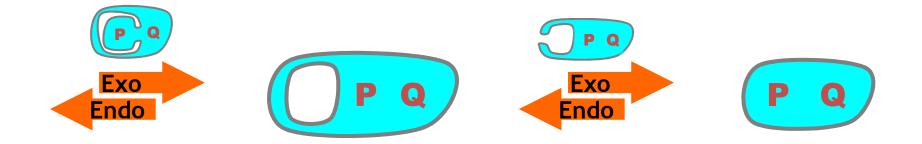


# The Membrane Machine "Instruction Set"



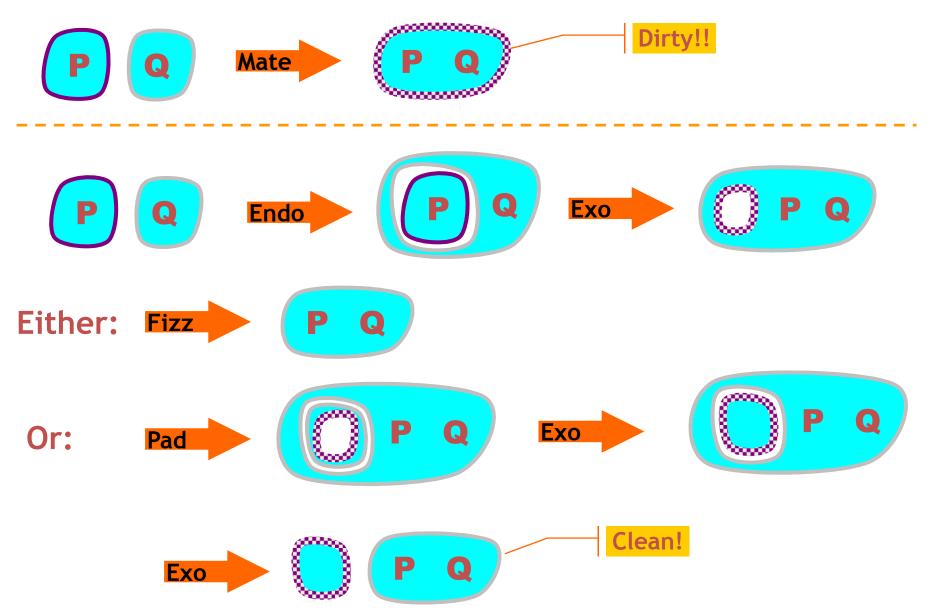
# Mito/Mate by 3 Endo/Exo



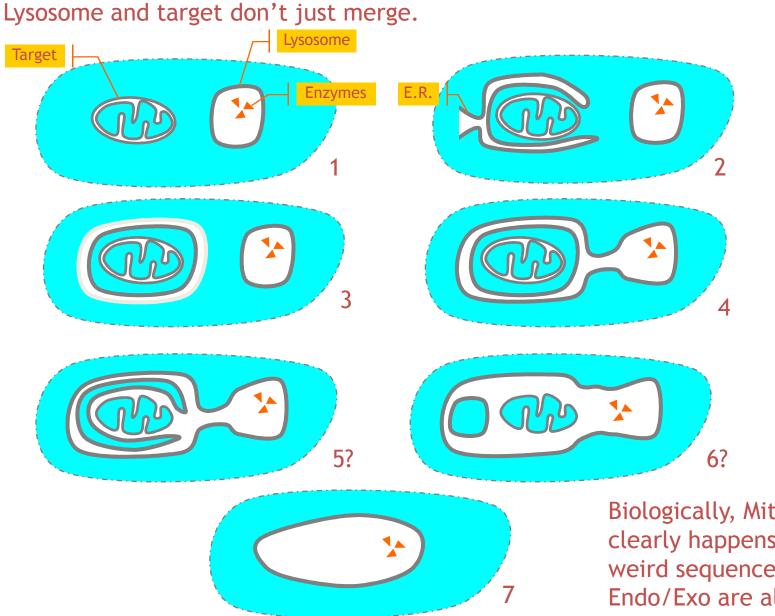


# (fake) Example: Clean Eating

(why Endo/Exo is "healthier" than Mito/Mate)

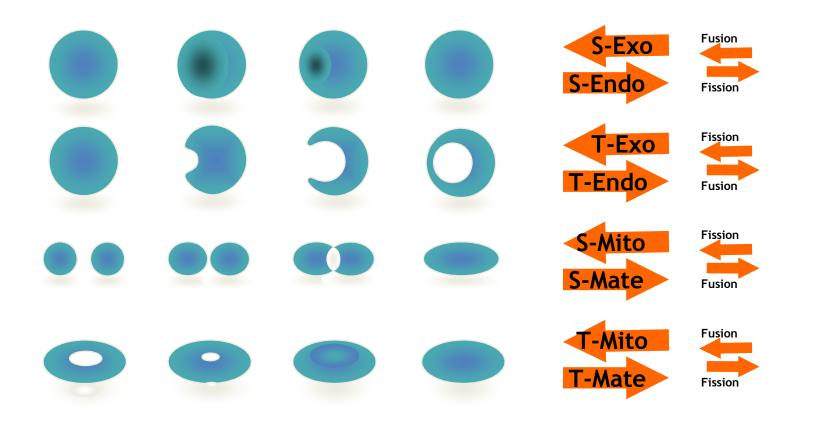


# **Example: Autophagic Process**



Biologically, Mito/Mate clearly happens. However, weird sequences of Endo/Exo are also common.

## ... in 3D

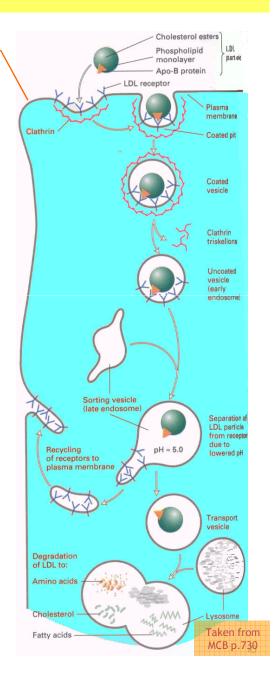


# **A Membrane Algorithm**

Lipid bilayer

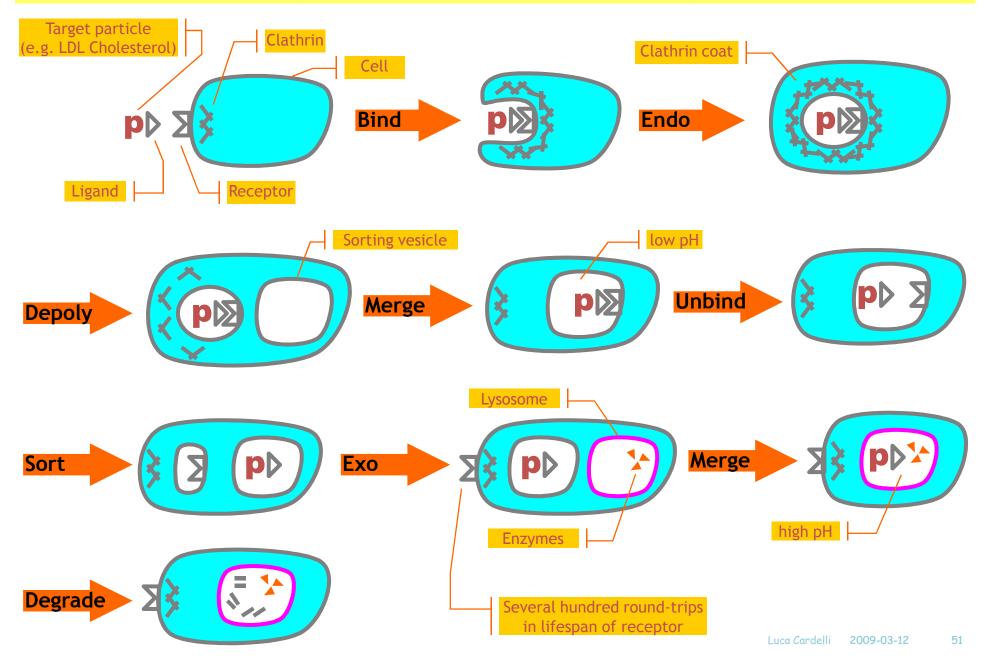
### • LDL-Cholesterol Degradation

- A cast of many thousands (molecules) just to get one molecule from A to B.
- Membranes are key to the algorithm, we want to model *them*, not their individual millions of molecules.
- Some very fancy chemistry
  - But its "purpose" is to reliably implement a specific sequence of discrete steps.

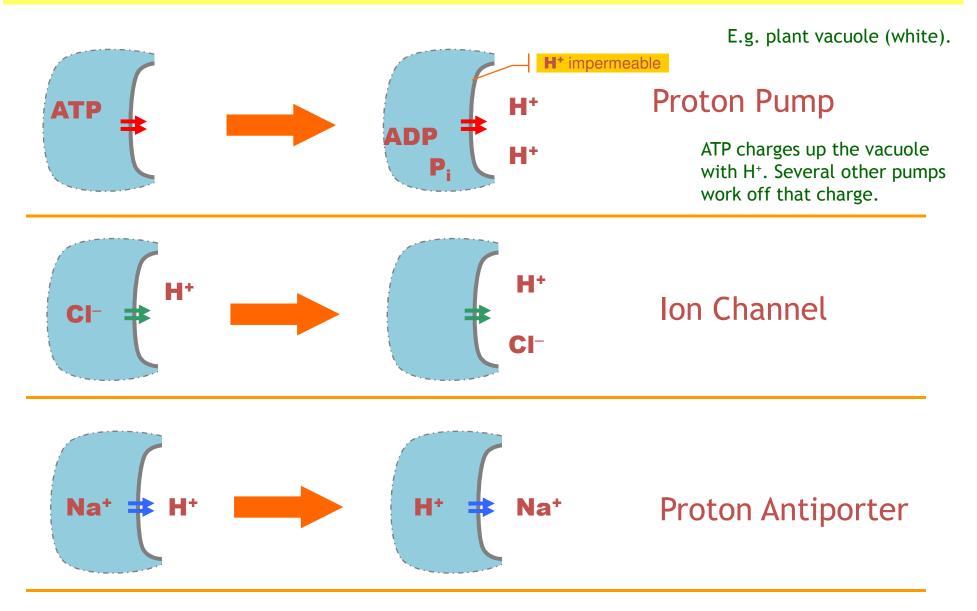


### A more C.S.-style state transition diagram

(Receptor-Mediate Degradation Pathway)



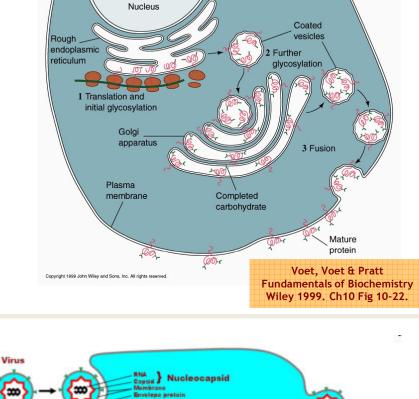
## **Operators** on Membranes



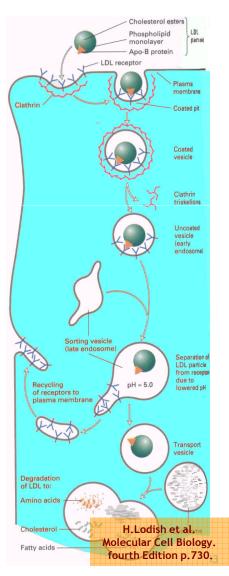
A plant vacuole has all those things on it, to accumulate NaCl.

# **Membrane Algorithms**

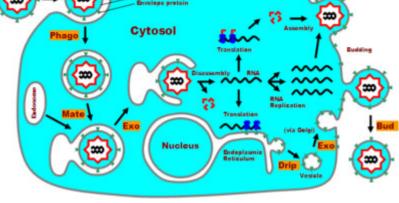
Protein Production and Secretion



LDL-Cholesterol Degradation



Viral Replication



Adapted from: B.Alberts et al. Molecular Biology of the Cell third edition p.279.

# Notations for the Membrane Machine

- "Snapshot" diagrams
  - In biology literature.

### • P-Systems

 G.Paun uses ideas from the theory of grammars and formal languages to model "Membrane Computing" (book 2002).

http://psystems.disco.unimib.it/.

#### • BioAmbients

- An extension of BioSPI along Ambient Calculus lines (with more bio-relevant mobility primitives) to model dynamic compartments.
- Brane Calculi
  - Computation *on* the membrane.